

# High Energy Rho Meson Leptoproduction<sup>§</sup>

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**Abstract:** We investigate the longitudinal and transverse polarized cross-sections of the leptoproduction of the  $\rho$  meson in the high energy limit. Our model is based on the computation of the impact factor  $\gamma^*(\lambda_\gamma) \rightarrow \rho(\lambda_\rho)$  using the twist expansion in the forward limit which is expressed in the impact parameter space. This treatment involves in the final stage the twist 2 and twist 3 distribution amplitudes (DAs) of the  $\rho$  meson and the dipole scattering amplitude. Taking models that exist for the DAs and for the dipole cross-section. We get a phenomenological model for the helicity amplitudes. We compare our predictions with HERA data and get a fairly good description for large enough virtualities of the photon.

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## 1. INTRODUCTION

We study the high energy diffractive leptoproduction of  $\rho$  meson

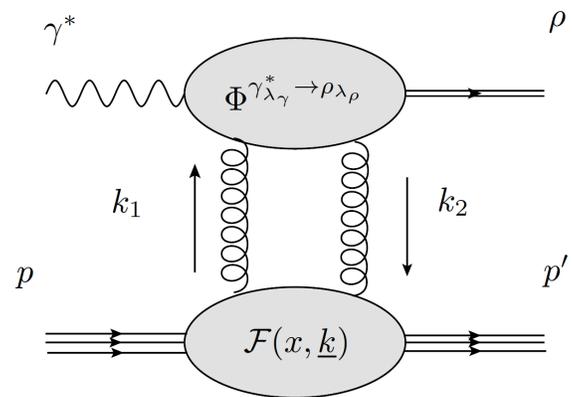
$$\gamma^*(q, \lambda_\gamma) N(p) \rightarrow \rho(p_\rho, \lambda_\rho) N(p'), \quad (1)$$

where  $N$  is the nucleon target,  $\lambda_\rho$  and  $\lambda_\gamma$  are respectively the polarizations of the  $\rho$  meson and of the virtual photon. The longitudinal and transverse polarized cross-sections  $\sigma_L$  and  $\sigma_T$  of the process (1) can be expressed in terms of the helicity amplitudes, which are denoted as  $T_{\lambda_\rho \lambda_\gamma}$ . In the limit of high energy in the center of mass of the  $\gamma^* N$  system, the helicity amplitudes can be factorized, using the  $k_T$ -factorization scheme, into the convolution of the impact factor  $\Phi^{\gamma^* \lambda_\gamma \rightarrow \rho \lambda_\rho}$  associated to the process

$$\gamma^*(q, \lambda_\gamma) g(k_1) \rightarrow \rho(p_\rho, \lambda_\rho) g(k_2), \quad (2)$$

and the unintegrated gluon density<sup>1</sup>  $\mathcal{F}(x, \underline{k})$ . In our kinematics we use the Sudakov decomposition along the light cone vectors  $p_1$  and  $p_2$ , such as

$$\begin{aligned} p_\rho &\sim p_1, \quad p \sim p_2, \quad q \sim p_1 - \frac{Q^2}{s} p_2, \\ s &= (q + p)^2 \sim 2p_1 \cdot p_2 \gg (Q^2, m_\rho^2). \end{aligned} \quad (3)$$



**Fig. (1).** Impact factor representation of the helicity amplitudes.

The  $t$ -channel gluon momenta, illustrated in Fig. (1), read  $k_1 = \frac{\kappa + Q^2 + k_\perp^2}{s} p_2 + k_\perp$  and  $k_2 = \frac{\kappa + k_\perp^2}{s} p_2 + k_\perp$ , where  $\kappa$  is the energy in the center of mass of the system  $\gamma^*(q)g(k_1)$ . The helicity amplitudes are written as:

$$T_{\lambda_\rho \lambda_\gamma} = is \int \frac{d^2 \underline{k}}{(k_\perp^2)^2} \Phi^{\gamma^* \lambda_\gamma \rightarrow \rho \lambda_\rho}(\underline{k}) \mathcal{F}(x, \underline{k}). \quad (4)$$

Assuming the virtuality of the photon  $Q$  ( $Q^2 = -q^2$ ) is large compared to the QCD scale  $\Lambda_{QCD}$ , the impact factors  $\Phi^{\gamma^* L \rightarrow \rho L}$  and  $\Phi^{\gamma^* T \rightarrow \rho L}$  were computed in ref. [1], using the

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<sup>1</sup>We denote by  $\underline{x}$  the 2-dimension euclidean vector associated to the Minkowskian  $x_\perp$ ,  $\underline{x}^2 = -x_\perp^2$ .

collinear factorization on the light-cone. In this approach, the impact factors are parameterized by the leading twist DA of the  $\rho$  meson. This computation was extended in refs. [2, 3]

to obtain the  $\Phi^{\gamma_T^* \rightarrow \rho_T}$  impact factor in the limit  $|t| \sim 0$ . In this last case, the leading twist 2 contribution does not exist and the amplitude is parameterized by the twist 3 DAs of the  $\rho$

meson. The result for  $\Phi^{\gamma_T^* \rightarrow \rho_T}$  obtained from the light-cone collinear factorization is the sum of two contributions: from a quark antiquark ( $q\bar{q}$ ) Fock state and from a quark antiquark gluon ( $q\bar{q}g$ ) Fock state. Relations between the DAs can be derived from the first principles of QCD and the twist 3 DAs that parameterize the Fourier transforms of the  $q\bar{q}$  correlators can be split into two solutions: the Wandzura-Wilczek (WW) solutions, which consist in neglecting the  $q\bar{q}g$  DAs, and the “genuine” solutions, that only depend on the  $q\bar{q}g$  DAs. Thus, one represent the  $q\bar{q}$

and the  $q\bar{q}g$  contributions to the impact factor  $\Phi^{\gamma_T^* \rightarrow \rho_T}$  as a sum of a WW contribution and of a genuine contribution. A first phenomenological model proposed in ref. [5] was based on the results of refs. [1, 3] and used a model for the proton impact factor inspired from ref. [4]. The results of this study have led to the conclusion that the soft  $t$ -channel gluons have a sizable contribution, which calls for the implementation of the saturation effects in this perturbative approach.

For this aim, in ref. [6], we have performed calculations of the twist 2 and twist 3 impact factors in the impact parameter space. We have shown also the equivalence of obtained results with the ones in momentum space of ref. [3]. The results in the impact parameter representation can be put in the form

$$\Phi^{\gamma_L^* \rightarrow \rho_L}(\underline{k}, Q, \mu^2) = \left( \frac{\delta^{ab}}{2} \right) \int dy \int d\underline{r} \psi_{(q\bar{q})}^{\gamma_L^* \rightarrow \rho_L}(y, \underline{r}; Q, \mu^2) \mathcal{A}(\underline{r}, \underline{k}), \quad (5)$$

$$\Phi^{\gamma_T^* \rightarrow \rho_T}(\underline{k}, Q, \mu^2) = \left( \frac{\delta^{ab}}{2} \right) \int dy \int d\underline{r} \psi_{(q\bar{q})}^{\gamma_T^* \rightarrow \rho_T}(y, \underline{r}; Q, \mu^2) \mathcal{A}(\underline{r}, \underline{k})$$

$$+ \left( \frac{\delta^{ab}}{2} \right) \int dy_2 \int dy_1 \int d\underline{r} \psi_{(q\bar{q}g)}^{\gamma_T^* \rightarrow \rho_T}(y_1, y_2, \underline{r}; Q, \mu^2) \mathcal{A}(\underline{r}, \underline{k}), \quad (6)$$

where the functions  $\psi_{q\bar{q}}^{\gamma_L^* \rightarrow \rho_L}$ ,  $\psi_{q\bar{q}}^{\gamma_T^* \rightarrow \rho_T}$  and  $\psi_{q\bar{q}g}^{\gamma_T^* \rightarrow \rho_T}$  are respectively our results for the transitions  $\gamma_L^* \rightarrow (q\bar{q}) \rightarrow \rho_L$ ,  $\gamma_T^* \rightarrow (q\bar{q}) \rightarrow \rho_T$  and  $\gamma_T^* \rightarrow (q\bar{q}g) \rightarrow \rho_T$ .  $\mathcal{A}(\underline{r}, \underline{k})$  is the scattering amplitude of a color dipole of transverse size  $\underline{r}$ , with the  $t$ -channel gluons having transverse momenta  $\underline{k}$ . In eqs. (5, 6)  $a$  and  $b$  are the color indices of the  $t$ -channel gluons in a singlet state. As a result, the well-known wave functions of the virtual photon factorize out in the expressions of  $\psi_{q\bar{q}}^{\gamma_L^* \rightarrow \rho_L}$  and  $\psi_{q\bar{q}}^{\gamma_T^* \rightarrow \rho_T}$ . The  $\rho$  meson non-perturbative parts are encoded by the twist 2 and twist 3 DAs and  $\mu$  stands for the factorization/renormalization scale of the DAs. We use the model of Ball, Braun, Koike and Tanaka developed in ref. [7] to get explicit expressions for

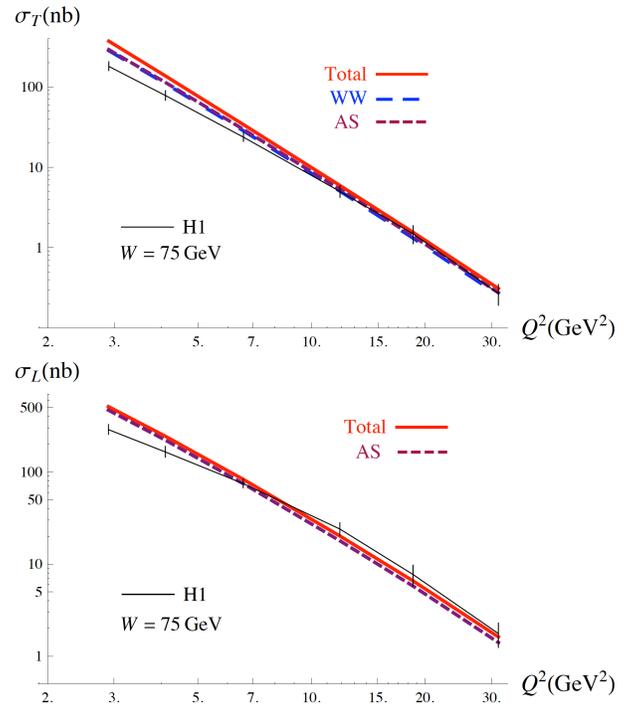
the DAs. This model relies on the conformal expansion of the DAs to separate the longitudinal momentum dependence from the scale dependence in  $\mu$ . It is customary to call “asymptotic” (AS) the results in the limit  $\mu^2 \rightarrow \infty$ . On the other hand, a natural choice for this scale is  $\mu^2 = (Q^2 + m_\rho^2)/4$ . Note that the factorization of the dipole scattering amplitude  $\mathcal{A}(\underline{r}, \underline{k})$  is due to the relations between the DAs coming from the equations of motion of QCD.

Inserting the expressions (5, 6) for the impact factor in eq. (4) leads to

$$\frac{T_{00}}{s} = \int dy \int d\underline{r} \psi_{(q\bar{q})}^{\gamma_L^* \rightarrow \rho_L}(y, \underline{r}; Q, \mu^2) \hat{\sigma}(x, \underline{r}), \quad (7)$$

$$\frac{T_{11}}{s} = \int d\underline{r} \left[ \int dy \psi_{(q\bar{q})}^{\gamma_T^* \rightarrow \rho_T}(y, \underline{r}; Q, \mu^2) + \int dy_2 \int dy_1 \psi_{(q\bar{q}g)}^{\gamma_T^* \rightarrow \rho_T}(y_1, y_2, \underline{r}; Q, \mu^2) \right] \hat{\sigma}(x, \underline{r}), \quad (8)$$

where  $\hat{\sigma}(x, \underline{r})$  is the dipole cross-section. These expressions are the starting point for our phenomenological analysis.



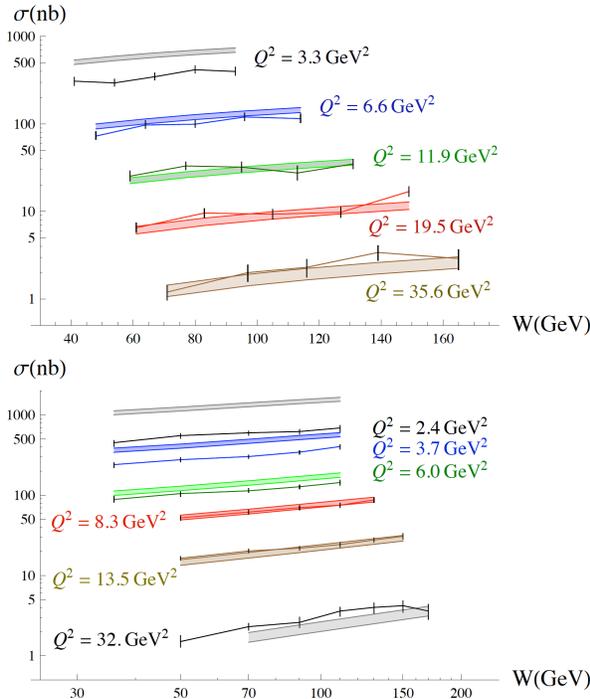
**Fig. (2).** Left: Total, WW and AS contributions to  $\sigma_T$  vs  $Q^2$ , compared to H1 [9] data. Right: Total and AS twist 2 contributions to  $\sigma_L$  vs  $Q^2$  compared to H1 data.

## 2. CONFRONTING OUR PREDICTIONS WITH HERA DATA

In ref. [8], we have compared our predictions for the transverse and longitudinal polarized cross-sections, shown in Fig. (2), with the data from H1 [9]. These predictions are obtained using the dipole scattering amplitude of ref. [10], which is based on numerical solutions of the running coupling Balitsky-Kovchegov (rcBK) equation [11]. This model of dipole scattering amplitude allows to account for the saturation

effects in our description of the  $\rho$  meson leptoproduction. Note that as we use a model of dipole cross-section already fitted on inclusive structure functions then we do not need to adjust value of any parameter. The results are in good agreement with the data for  $Q^2 \gtrsim 5 \text{ GeV}^2$  and they are weakly dependent on the choice of the factorization/renormalization scale  $\mu$ . The discrepancy for smaller virtualities  $Q^2 \gtrsim 5 \text{ GeV}^2$  indicates that higher twist corrections to the impact factors can become important for such values of  $Q^2$ .

In Fig. (3), we show our predictions for the total cross-section  $\sigma$  of the diffractive leptoproduction of  $\rho$  meson and compared then with the data of H1 [9] and ZEUS [12], as a function  $W$ . The  $W$ -dependence of our predictions is given by the dipole cross-section model [10]. In this way we obtain a good agreement between the predictions and the data for the  $W$ -dependence.



**Fig (3).** Predictions for the total cross-section  $\sigma$  vs  $W$  compared to H1 [9] (left) and ZEUS [12] (right) data.

## CONCLUSION

The success of the model we have presented to describe the  $W$ - and the  $Q^2$ -dependencies with the proper normalizations for large enough  $Q^2$ , relies on the computations from first principles of the impact factors  $\Phi_{\gamma^* \rightarrow \rho}$  and the models for the twist 2 and twist 3 DAs as well as the model for the dipole scattering amplitude. Consequently, this approach constitutes a good way to unravel the non-perturbative aspects of the leptoproduction of

the  $\rho$  meson. The perspectives of this study are numerous, as it could be extended in the non-forward kinematics and for other helicity amplitudes. This could allow to probe the impact parameter dipole/nucleon target dependence of the dipole scattering amplitudes. The higher twist correction effects could lead to a better description of the data for lower values of  $Q^2$  closer to the saturation scale in the HERA kinematics.

## CONFLICT OF INTEREST

The authors confirm that this article content has no conflicts of interest.

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